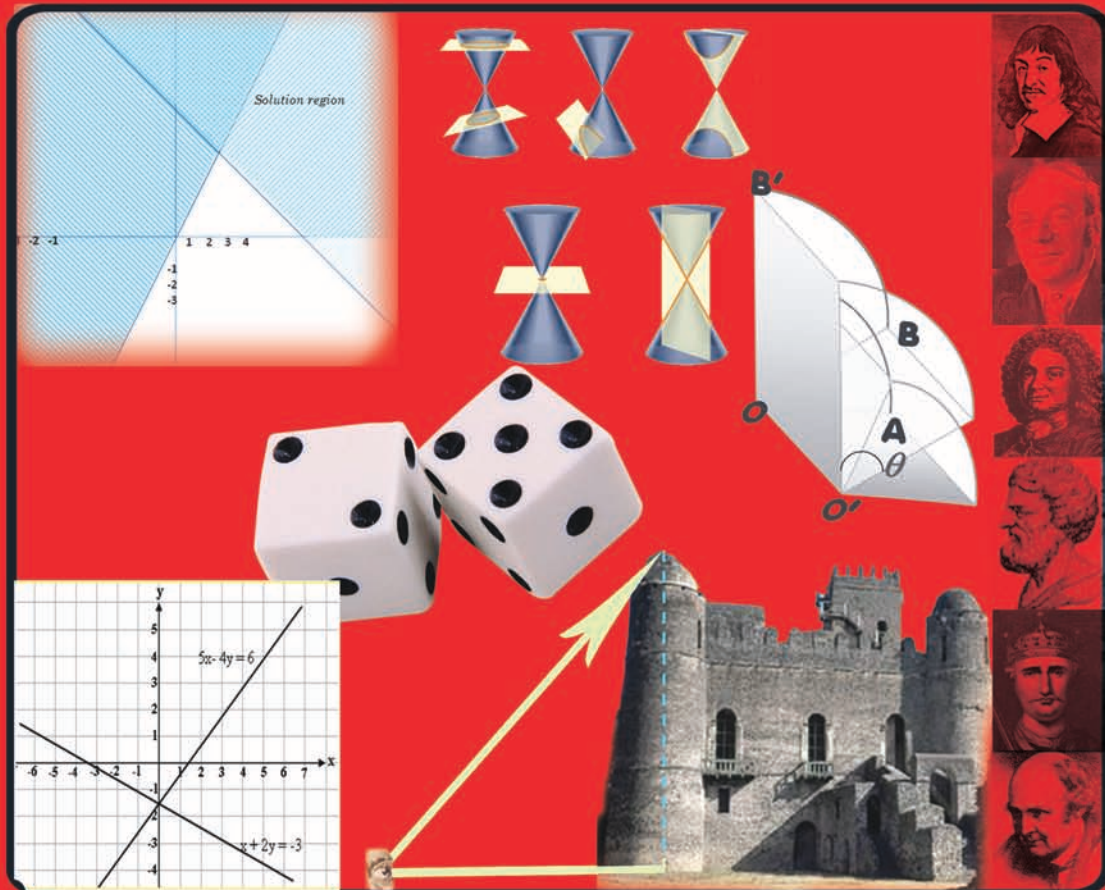




# MATHEMATICS

STUDENT TEXTBOOK  
GRADE **11**



FEDERAL DEMOCRATIC REPUBLIC OF ETHIOPIA  
MINISTRY OF EDUCATION

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# MATHEMATICS

## STUDENT TEXTBOOK

### GRADE 11

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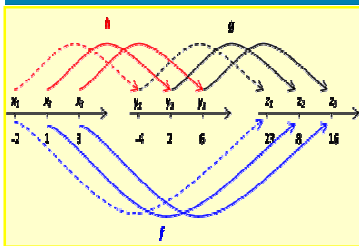
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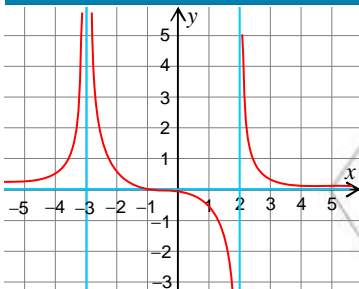
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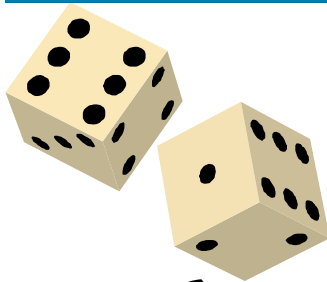


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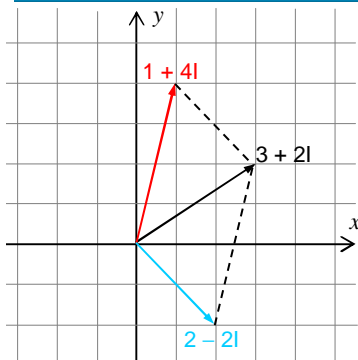
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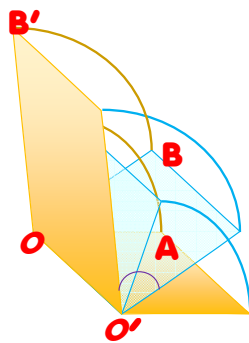
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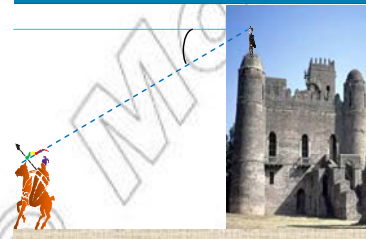
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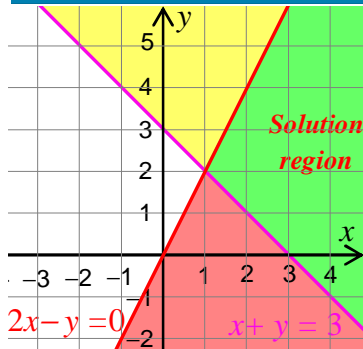
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